3944

## Accurate High-speed 3D-Registration of EPI vNavs for Head Motion Correction

Yingzhuo Zhang ${ }^{1}$, Iman Aganj ${ }^{2,3}$, André J.W. van der Kouwe ${ }^{2,3}$, and Matthew Dylan Tisdall ${ }^{4}$
${ }^{1}$ John A. Paulson School of Engineering and Applied Sciences, Harvard University, Cambridge, MA, United States, ${ }^{2}$ Athinoula A. Martinos Center for Biomedical Imaging, Radiology Department, Massachusetts General Hospital, Charlestown, MA, United States, ${ }^{3}$ Department of Radiology, Harvard Medical School, Boston, MA, United States, ${ }^{4}$ Department of Radiology, Perelman School of Medicine, University of Pennsylvania, Philadelphia, PA, United States

## Synopsis

Low-resollution, wholle-head volumes can be acquired rapidlly with $\mathbb{E P I}$-based volumetric mavigators (vNavs). vNavs interspersed iim a llonger scam are widely used for prospective motion correction in a variety of sequences. To further improve the accuracy and fllexibiliity of vNavs, we present a novell registration algoriithm, tailored specificallly for the vNavs application. Accuracy of the algoriithm is tested on navigator volumes acquired with humam volunteers at three isotropic resolutions, $6.4 \mathrm{~mm}_{n} 8 \mathrm{~mm}$, and 10 mm , usimg a series of field of view (FOV) rotations and translations to provide ground truth rigid "motion"'.

## Purpose

Volumetric navigators (vNavs) ${ }^{1,2}$, based on 3D-encoded gradient echo EPI, are widely used prospective motion correction systems for neuroimaging, particularly in pediatric imaging. Previous applications of vNavs used the PACE ${ }^{3}$ registration algorithm, designed for higher-resolution fMRI volumes, constraining vNav design choices. In this work, we present a novel registration algorithm, achieving both the accuracy and efficiency requirements of prospective motion correction with lower-resolution, and thus faster, vNavs than PACE allowed.

## Method

Imaging was performed on a 3 T TIM Trio (Siemens Healthcare, Erlangen, Germany), using the body coil to ensure spatial uniformity. Three human volunteers, having given informed consent, were scanned at three isotropic resolutions, $6.4 \mathrm{~mm}, 8 \mathrm{~mm}$, and 10 mm (see acquisition parameters in Table 1).

Motion was simulated by a programmed series of FOV rotations and translations. "Small rotations" data contained a volume at iso-center and on-axis (the "reference"), followed by volumes with rotations of $0.5^{\circ}-5^{\circ}$ at $0.5^{\circ}$ increments and translations of $1-5 \mathrm{~mm}$ at 1 mm increments. "Large rotations" data was acquired on two of the volunteers with rotations of $5^{\circ}-25^{\circ}$ at $5^{\circ}$ increments. Rotations were repeated around the $x-, y$-, and $z$-axes paired with $z$-direction translations, and around axes oriented along $x y, x z$, and $y z$ paired with $x y$-direction translations. Scans were acquired in $<30$ s sets, during which the volunteers were instructed to hold their breath and remain still. 432 volumes per resolution per subject were acquired, from which 420 pairs (comparing each set's "reference" with subsequent volumes) were extracted.

The volumes were masked before registration with a spherical mask (radius = image width/2-1 pixels) in the Fourier domain. Corners of the mask were Hann windowed to reduce ringing artifacts.

Our algorithm registers a new volume $V_{N}(\boldsymbol{x})$ to a given reference volume $V_{R}(\boldsymbol{x})$ by minimizing the residual

$$
r(\boldsymbol{p})=\left|\left\{\boldsymbol{W}(T(\boldsymbol{p}, \boldsymbol{x}))\left[V_{N}(\boldsymbol{x})-V_{R}(T(\boldsymbol{p}, \boldsymbol{x}))\right] \mid \boldsymbol{x} \in \boldsymbol{X}\right\}\right|_{2}
$$

where $T(\boldsymbol{p}, \boldsymbol{x})$ is a rigid transformation parameterized by $\boldsymbol{p} \in R^{6} . \boldsymbol{W}(\boldsymbol{x})$ is the same mask function initially applied in the Fourier domain, and $\boldsymbol{X}$ is the set of points inside our image FOV. We transform the reference to the new volume, interpolating only the reference volume. We can then precompute the coefficients of the cubic B-spline interpolator, accelerating each interpolation step ${ }^{4,5}$.

We performed Gauss-Newton minimization, giving the update equation

Figures

|  | 6.4 mm | 8 mm | 10 mm |
| :---: | :---: | :---: | :---: |
| TR | 15 ms | 11 ms | 10 ms |
| TE | 6.7 ms | 5.0 ms | 4.1 ms |
| FA | $3^{\circ}$ | $3^{\circ}$ | $3^{\circ}$ |
| BW | $4310 \mathrm{~Hz} / \mathrm{Px}$ | $4596 \mathrm{~Hz} / \mathrm{Px}$ | $4578 \mathrm{~Hz} / \mathrm{Px}$ |
| FOV | 256 mm | 256 mm | 260 mm |
| Total Scan Time | 600 ms | 352 ms | 260 ms |

Table 1. Scanner Parameters for vNavs.


Figure 1. Sagittal slices from vNavs at different resolutions.


Figure 2. Distribution of RMS error displacement on three different subjects with small rotations at three vNav resolutions. Each violin represents results from 420 pairs of registration with rotations ranging from 0 to 5 degrees and translation from 1 to 5 mm . Median value is shown as a white point in each violin, and on the left side of each violin is the scatter plot of the values of RMS error.


Figure 3. Distribution of RMS error displacement on two different subjects with large rotations at three vNav resolutions. Each violin represents results from 420 pairs

$$
\frac{\mathrm{d} r(\boldsymbol{p})^{T}}{\mathrm{~d} \boldsymbol{p}} \frac{\mathrm{~d} r(\boldsymbol{p})}{\mathrm{d} \boldsymbol{p}} \delta \boldsymbol{p}=-\frac{\mathrm{d} r(\boldsymbol{p})^{T}}{\mathrm{~d} \boldsymbol{p}} r(\boldsymbol{p})
$$

We update our estimated $\boldsymbol{p}$ by composing its transformation with that given by $\delta \boldsymbol{p}$. A line search scales $\delta \boldsymbol{p}$, ensuring the residual decreases at each step. Minimization stopped when updates move all points in a 100 mm radius of the image center less than 0.05 mm .

We evaluate the gradient with the approximation

$$
\frac{\mathrm{d} r(\boldsymbol{p})}{\mathrm{d} \boldsymbol{p}} \approx-\boldsymbol{W}(T(\boldsymbol{p}, \boldsymbol{x})) \frac{\mathrm{d} V_{N}(\boldsymbol{x})}{\mathrm{d} \boldsymbol{x}} \boldsymbol{M}(\boldsymbol{x}),
$$

where
and

$$
\boldsymbol{M}(\boldsymbol{x})=\left[\begin{array}{cccccc}
1 & 0 & 0 & 0 & x_{z} & -x_{y} \\
0 & 1 & 0 & -x_{z} & 0 & -x_{x} \\
0 & 0 & 1 & x_{y} & -x_{x} & 0
\end{array}\right]
$$

$$
\boldsymbol{x}=\left\{x_{x}, x_{y}, x_{z}\right\}
$$

We computed the "residual error transformation" between the estimated transformation and the known true transformation of each reference/new pair. We computed the RMS displacement that the "error transformation" would produce in a 100 mm sphere centered at isocenter ${ }^{6}$.

## Results and Discussion

In all conditions RMS error was within 1 mm , with the exception of large rotations for one subject at 8 mm resolution (Detailed results in Figures 2 and 3). We compared vNav resolutions using the Wilcoxon signed-rank test on the RMS errors (Results in Table 2). While 6.4 mm resolution produced the highest accuracy, assuming our motion tracking goal is $\sim 1 \mathrm{~mm}$, our new algorithm achieved functionally equivalent accuracy with $10 \mathrm{~mm} v \mathrm{Navs}$, requiring less than half of the acquisition time of 6.4 mm vNavs.

The algorithm is implemented in C++, using the Eigen ${ }^{7}$ library and is available on Github ${ }^{8}$. Median registration times for small rotations, running single-threaded on a 2.30 GHz Intel Xeon, were 12.97 $\mathrm{ms}, 25.10 \mathrm{~ms}$, and 54.53 , ms for $10 \mathrm{~mm}, 8 \mathrm{~mm}$, and 6.4 mm vNavs respectively. Large rotations took $18.30 \mathrm{~ms}, 36.46 \mathrm{~ms}$, and 88.47 ms , respectively.

To ensure that involuntary motion did not dominate registration error, we performed the same tests using a pineapple. Median RMS error in human subjects were $0.18,0.14,0.12$, and in pineapple were $0.23,0.21,0.19$, at $10 \mathrm{~mm}, 8 \mathrm{~mm}$ and 6.4 mm resolutions, respectively.

## Conclusions

We have developed and validated novel registration algorithm for vNavs that achieves fast and highly accurate motion tracking on a wider range of vNav protocols than was previously possible. Our algorithm supports motion correction with $10 \mathrm{~mm} v N a v s$, reducing navigator durations compared to previous designs, and increasing the number of sequences in which vNavs can be inserted.

## Acknowledgements

This work was funded by NIH awards: R00HD074649, R21AG046657, R01HD071664, R21EB008547, P41RR014075, R01HD085813, K01DK101631, and the BrightFocus Foundation (A2016172S).
of registration with rotations ranging from 5 to 25 degrees and translation from 1 to 5 mm . Median value is shown as a white point in each violin, and on the left side of each violin is the scatter plot of the values of RMS error.

|  | 8 mm to 6.4 mm | 10 mm to 6.4 mm | 10 mm to 8 m |
| :--- | :---: | :---: | :---: |
| Small Rotations | -3.49 | -10.38 | -7.33 |
| Large Rotations | -9.45 | -6.85 | 3.77 |

Table 2. Z-score computed from the Wilcoxon signed-rank test statistic for comparing registration accuracy across resolutions. The test was performed on each pair of vNav resolutions on small and large rotations. The test statistic is computed on the pairs of registration on all subjects combined. A negative score indicates that there is an improvement in the pair from the first resolution to the second, and a positive score indicates the opposite. All values in the table are $z$-scores that are significant for a one-sided difference at $p$ < 0.01 .

## References

1. Tisdall, M. Dylan, Aaron T. Hess, Martin Reuter, Ernesta M. Meintjes, Bruce Fischl, and André JW van der Kouwe. "Volumetric navigators for prospective motion correction and selective reacquisition in neuroanatomical MRI." Magnetic resonance in medicine 68, no. 2 (2012): 389-399.
2. Hess, Aaron T., M. Dylan Tisdall, Ovidiu C. Andronesi, Ernesta M. Meintjes, and André JW van der Kouwe. "Real-time motion and B0 corrected single voxel spectroscopy using volumetric navigators." Magnetic resonance in medicine 66, no. 2 (2011): 314-323.
3. Thesen, Stefan, Oliver Heid, Edgar Mueller, and Lothar R. Schad. "Prospective acquisition correction for head motion with image-based tracking for real-time fMRI." Magnetic Resonance in Medicine 44, no. 3 (2000): 457-465.
4. Lekien, Francois, and J. Marsden. "Tricubic interpolation in three dimensions." International Journal for Numerical Methods in Engineering 63, no. 3 (2005): 455-471.
5. Zhang, Yingzhuo, Iman Aganj, Andre J. van der Kouwe, and M. Dylan Tisdall. "Effects of Resolution and Registration Algorithm on the Accuracy of EPI vNavs for Real Time Head Motion Correction in MRI." Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition Workshops, pp. 143-151. 2016.
6. Jenkinson, Mark. "Measuring transformation error by RMS deviation." Studholme, C., Hill, DLG, Hawkes, DJ (1999).
7.G. Guennebaud, B. Jacob, et al. Eigen v3. http://eigen.tuxfamily.org, 2010.
7. Zhang, Yingzhuo, GitHub repository https://github.com/zyzdiana/MotionCorrection
[^0]
[^0]:    Proc.. \|mtll.. Soc.. Maqy.. Resom.. Med.. 25 ((20177))

